Using Trixi.jl for Adaptively Coupling Multiphysics Problems

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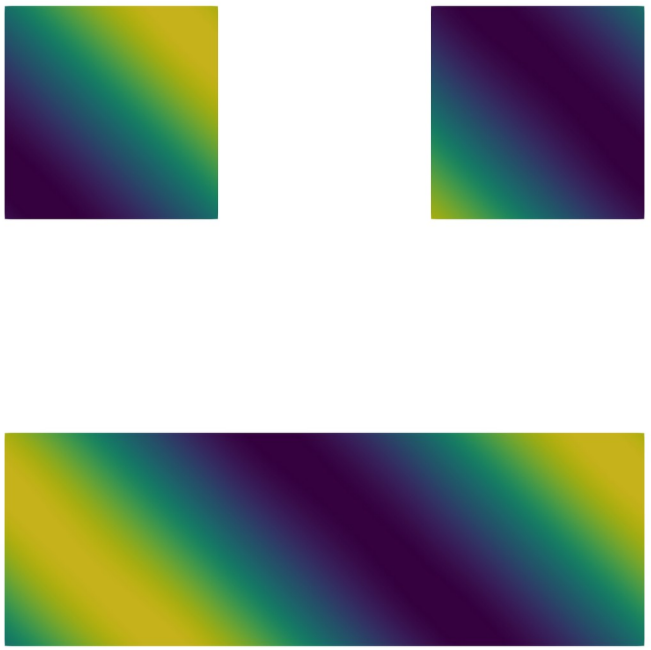
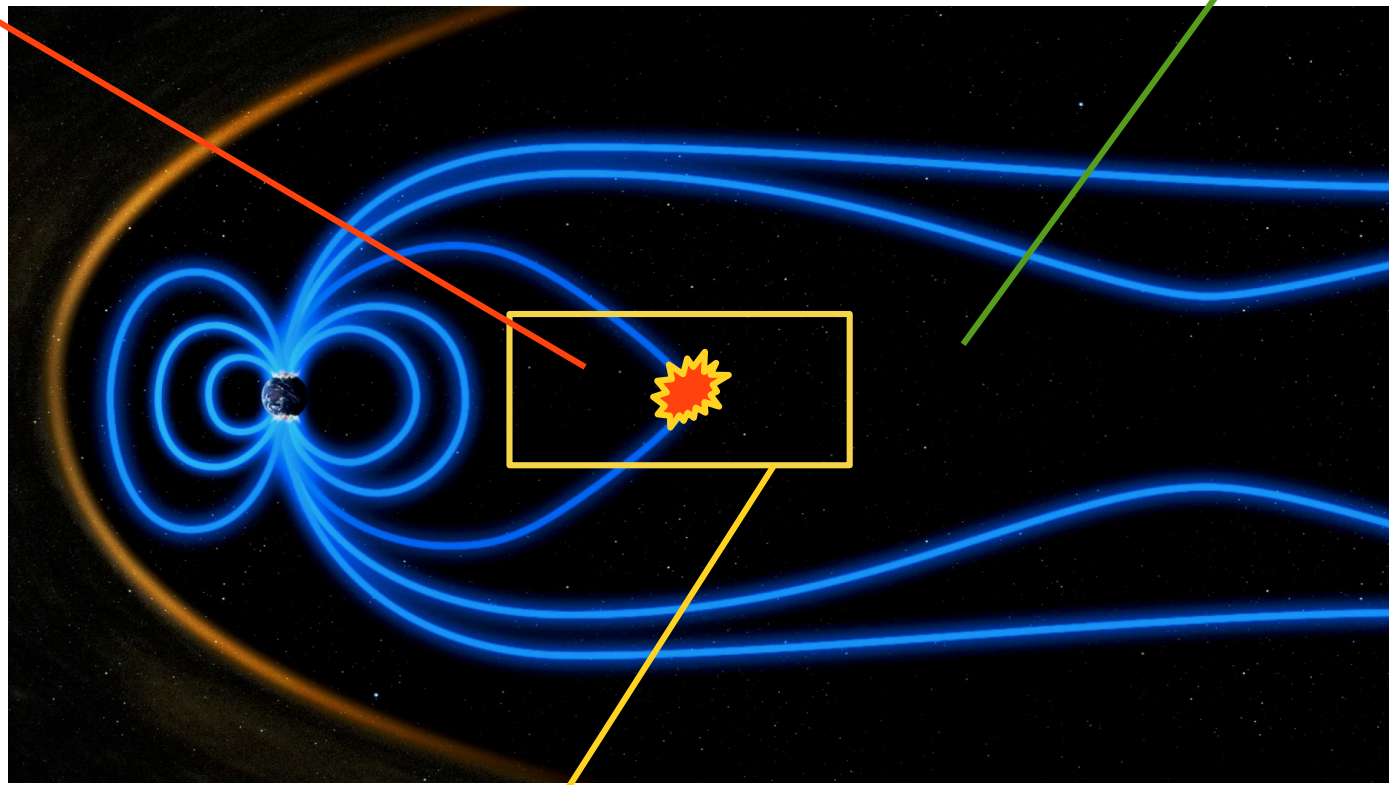


Universität
Augsburg
University

Modeling

kinetic model
(expensive)

magnetohydrodynamics (MHD)
(cheap)



(ESA)

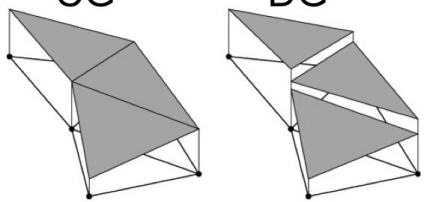
interface coupling

Trixi.jl

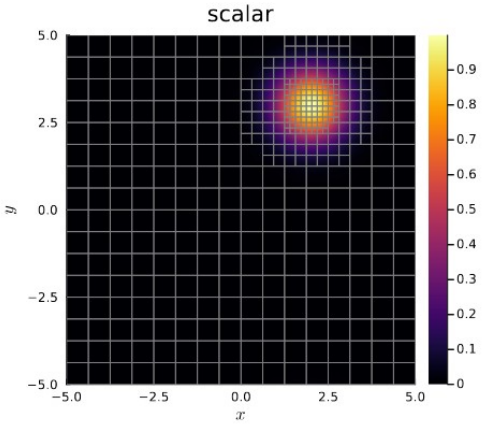
open source:
github.com/trixi-framework/Trixi.jl

Discontinuous Galerkin

CG DG

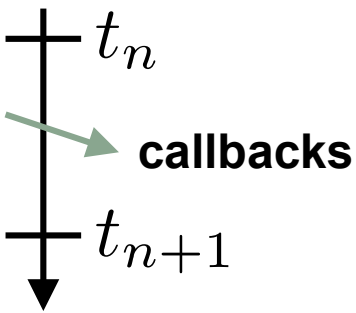


(Stack Overflow)



AMR

julia

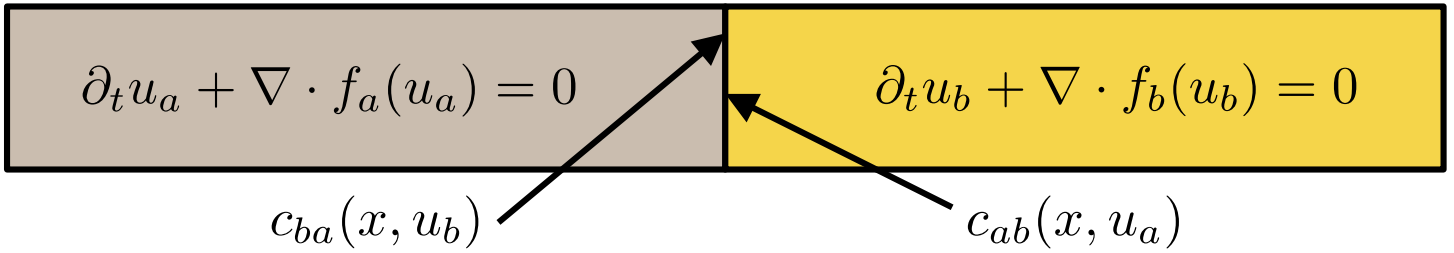


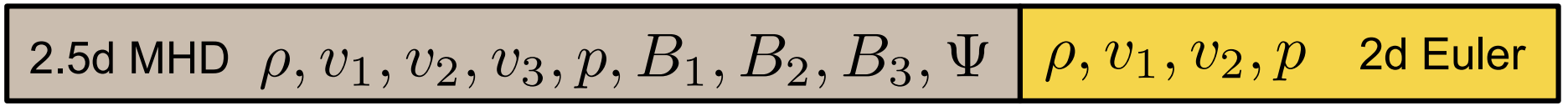
OrdinaryDiffEq (SciML)

```
using Trixi

equations = LinearScalarAdvectionEquation2D((0.5, -0.3)
solver = DGSEM(polydeg = 3)
cells_per_dimension = (16, 16)

mesh = StructuredMesh(cells_per_dimension, (-1, -1), (1, 1))

semi = SemidiscretizationHyperbolic(mesh, equations,
                                    initial_condition, solver)
ode = semidiscretize(semi, (0.0, 1.0));

stepsize_callback = StepsizeCallback(cfl = 1.6)
callbacks = CallbackSet(stepsize_callback)

sol = solve(ode, CarpenterKennedy2N54(),
            dt = 1.0, callback = callbacks);
```

Coupling via Converter Functions

Two system with any number of shared variables, including 0:

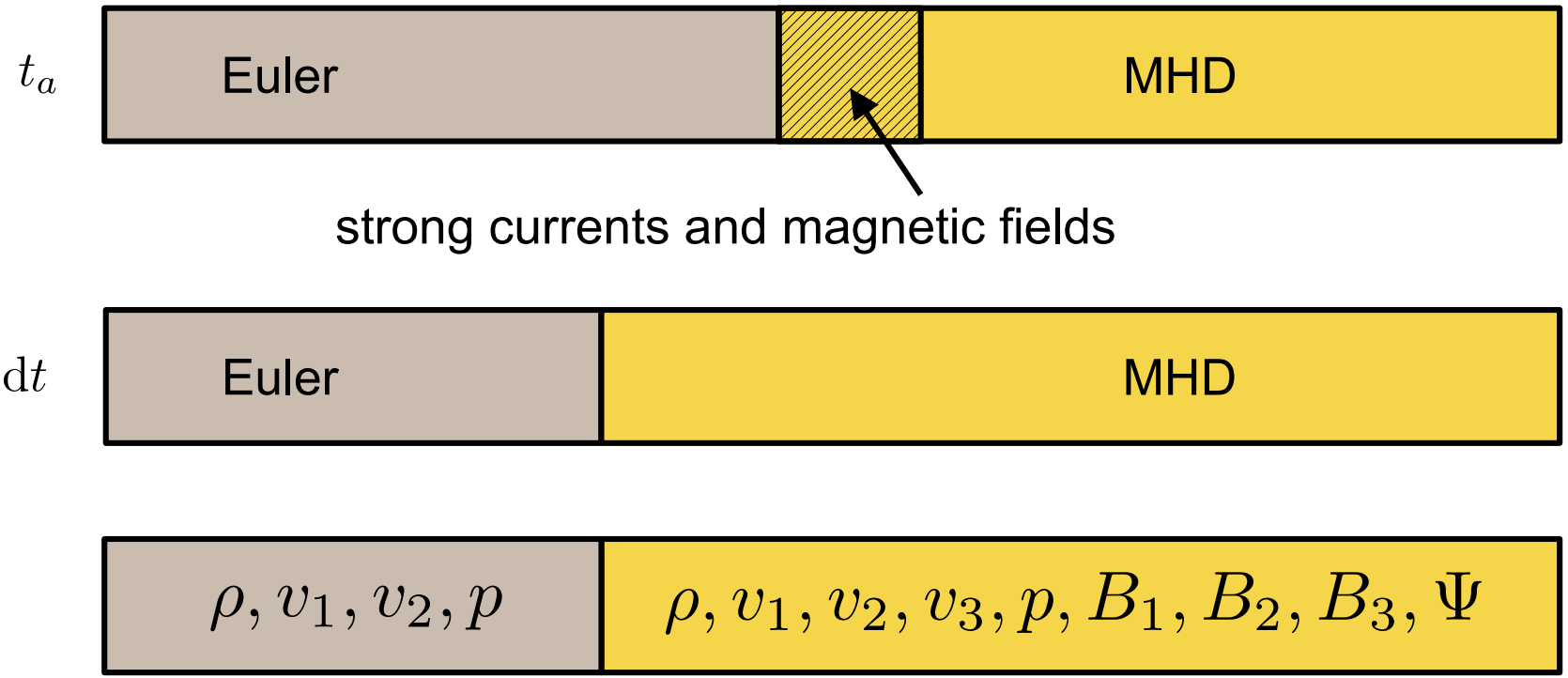





```
coupling_function12 = (x, u, equations_other, equations_own)
                      -> SVector(u[1], u[2], u[3], 0.0, u[4], 0.0, 0.0, 0.0, 0.0)
coupling_function21 = (x, u, equations_other, equations_own) -> SVector(u[1], u[2], u[3], u[5])
```

- User can define converter functions.
- Any pair of systems can be coupled.

Adaptive Coupling

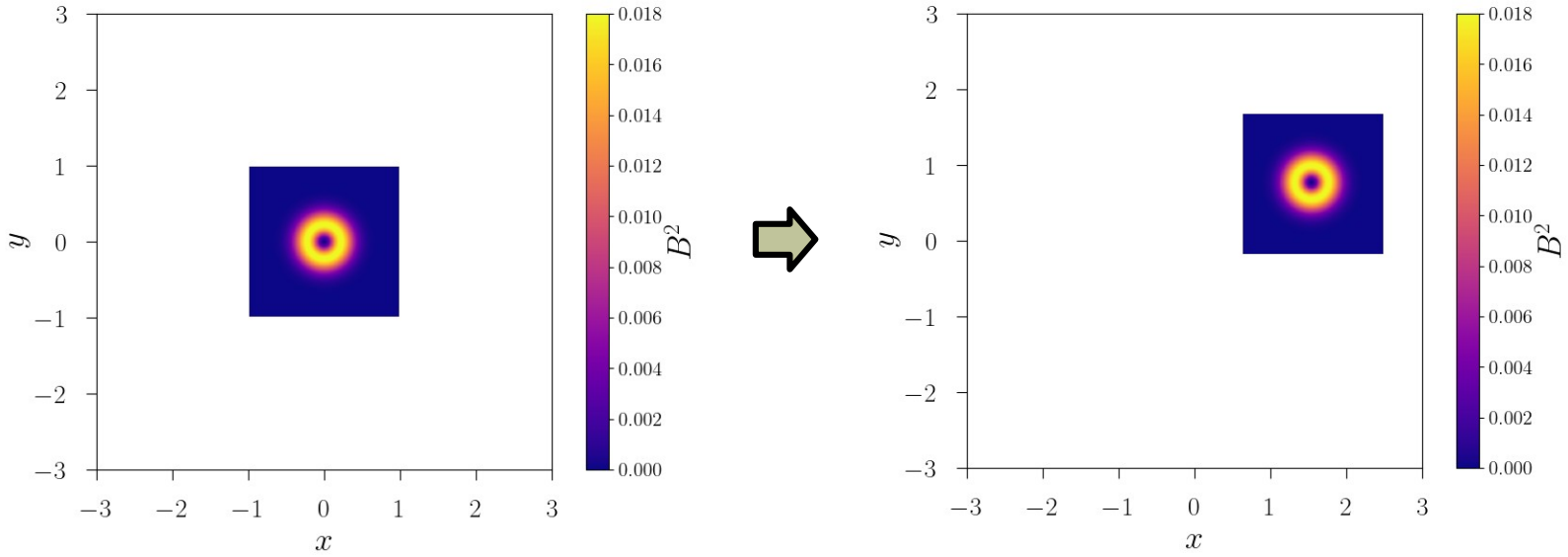


- Use callback functions to remesh.
- Use coupling functions to copy data.

Adaptive Model Selection

1. Generate the new grid (mesh views).
2. Write new u-solution vectors
3. Generate new ODE for OrdinaryDiffEq (integrator).
4. Reinitialize ODE integrator with new problem and new solution vector.

Euler and MHD



(movies)

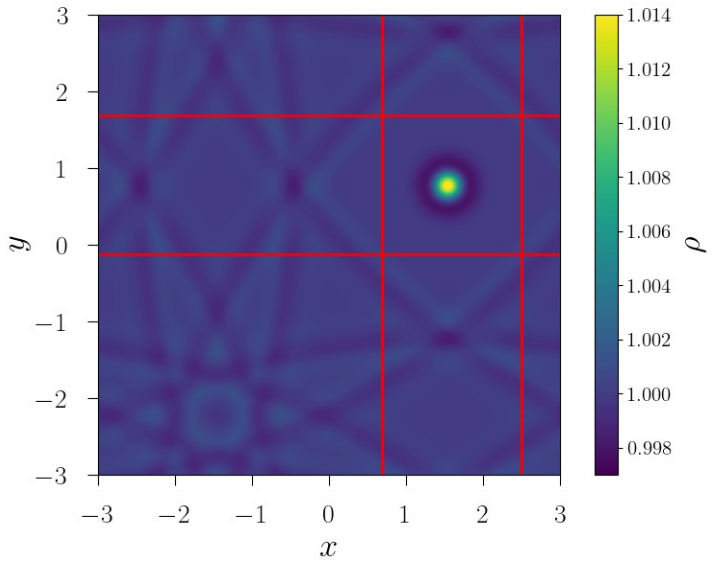
Time spent on coupled boundaries: 0.8%.

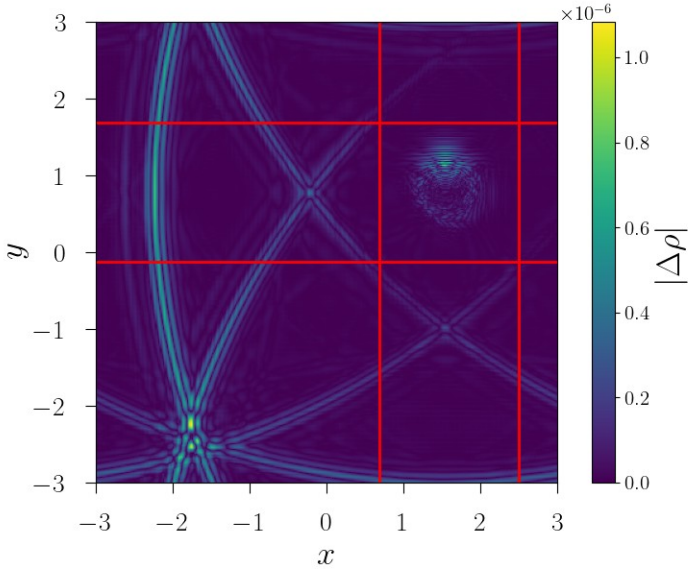
Time spent on model selection: 1.08s per model selection

Timings: coupled → 765.6s
full MHD → 1905.3s

Estimated maximum speed up: 3.31x; here: 2.49x

Density Evolution



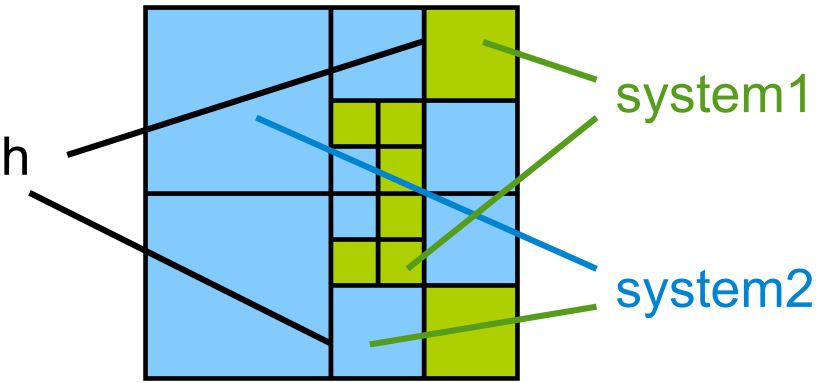


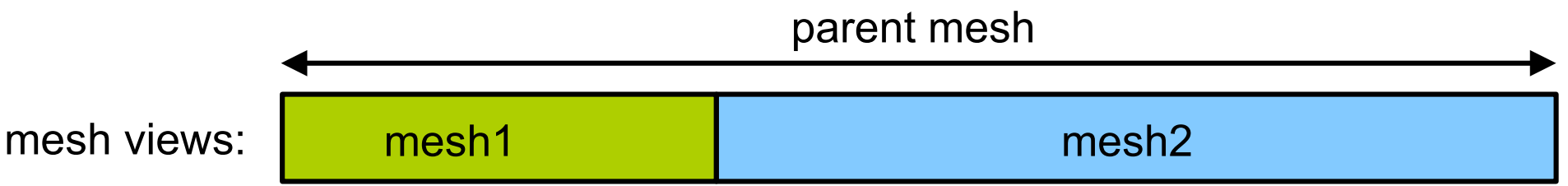
full MHD vs. coupled

- No artificial discontinuities.
- Small differences to full MHD simulation.

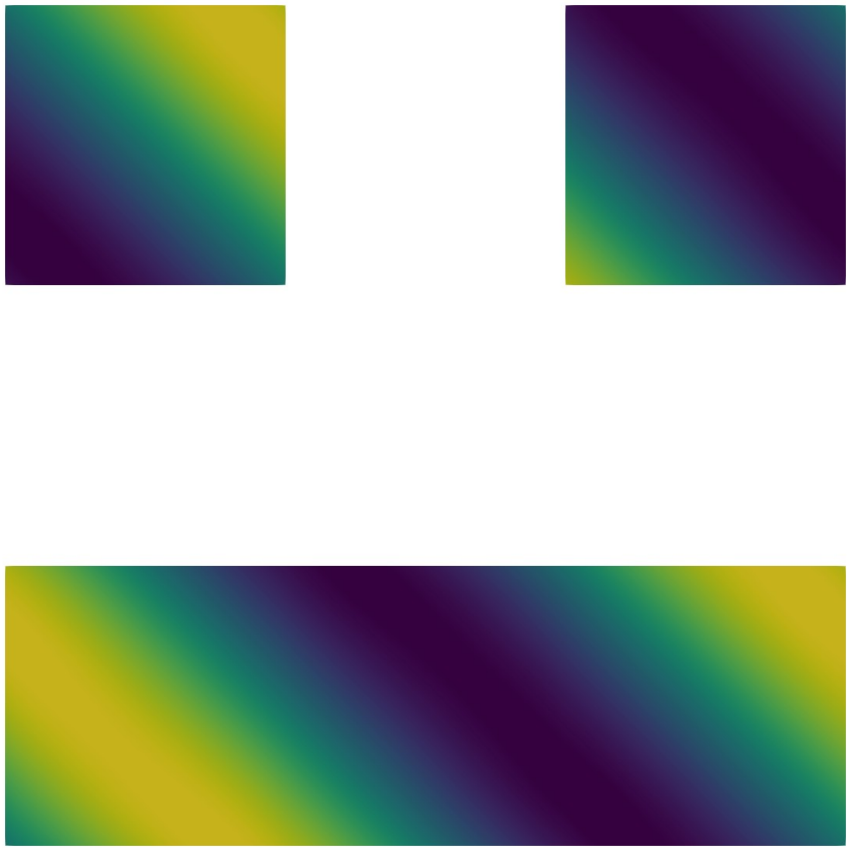
p4est Meshes

We can define the b.c. for each cell boundary.





p4est Meshes



- p4est mesh views in Trixi.jl
- arbitrary topology
- views on smallest (cell) scale
- no coupling implemented yet

Conclusion

- Flexible coupling through converter functions.
- Free domain definitions.
- Adaptive coupling with arbitrary criteria.
- Coupled hierarchy of models.
- Non-simply connected mesh views in p4est

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